



Algerian Space Agency  
Center of Space Techniques



## Optimal Choice for the Estimation of Precise GPS Stations Coordinates

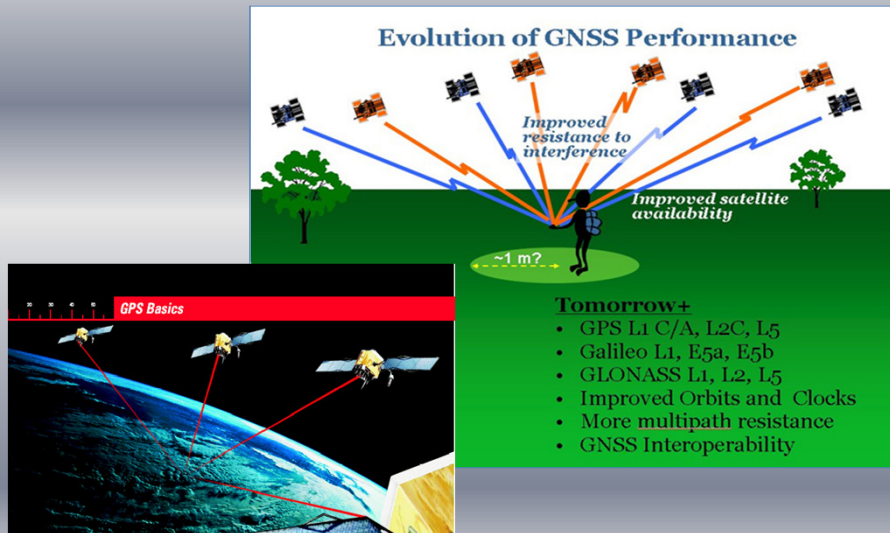
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FIG – Marrakech 2011

## Outline

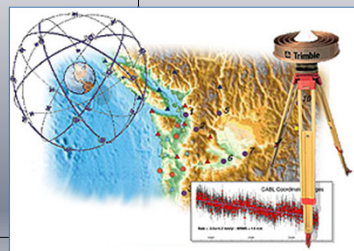
1. Introduction
2. the GPS signal in atmosphere
3. Theoretical Context of tropospheric delay
4. Processing and analyses of results
5. Conclusions and Perspectives

## Introduction



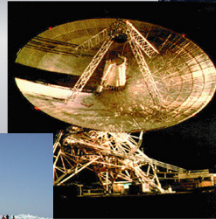
## The GPS

- **The Global Positioning System (GPS) is a satellite-based navigation system.**
- **GPS was originally intended for military applications, but in the 1980s, the government made the system available for civilian use.**
- **GPS works in any weather conditions, anywhere in the world, 24 hours a day. There are no subscription fees or setup charges to use GPS**
- **Some civilian uses:**
  - Navigation on land, sea, air and space
  - Geophysics research
  - Guidance systems
  - Geodetic network densification
  - Hydrographic surveys



## Three Parts

- Space segment
- Control segment
- User segment



## Principles

- The GPS system operates on the principles of trilateration, determining positions from distance measurements.
- This can be explained using the velocity equation.

$$\text{Velocity} = \frac{\text{Distance}}{\text{Time}}$$

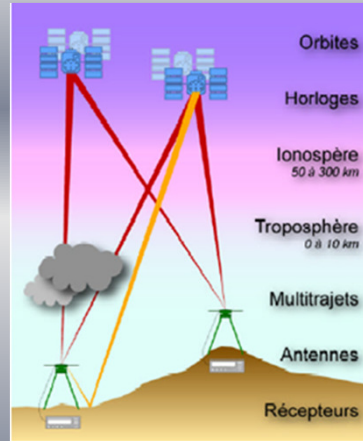
- Rearranging the equation for distance:

$$\text{Distance} = \text{Velocity} \times \text{Time}$$

- If the system knows the velocity of a signal and the time it takes for the signal to travel from the sender to the receiver, the distance between the sender and the receiver can be determined.

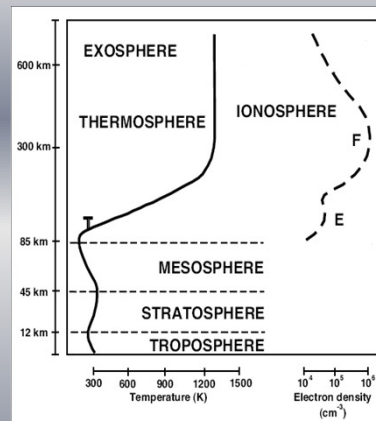
## Errors affected GPS signal

- IONOSPHERE
- TROPOSPHERE
- MULTIPATH
- SATELLITE CONFIGURATION/GEOMETRY (DOP)
- CLOCKS
- MONUMENTS
- ORBITS



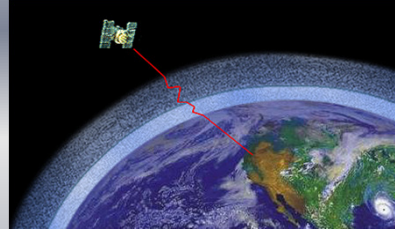
## The Signal GPS in Atmosphere

- Refractive zones of the atmosphere:
  - Ionosphere
  - Troposphere
- Impact on GPS Signals:
  - Non-linear path
  - Signal Slowdown
  - Increased travel time satellite-receiver: **Delay**



## Tropospheric Effects

- The troposphere is extending from the earth to 50 kilometres
- The troposphere is a non-dispersive medium for signal frequencies below 30 GHz.
- The Tropospheric error cannot be effectively reduced by dual-frequency GPS observations as used to eliminate the ionospheric error.



For further details See Leick (1995)

## Tropospheric Delay

(1) – Physical origin and equation

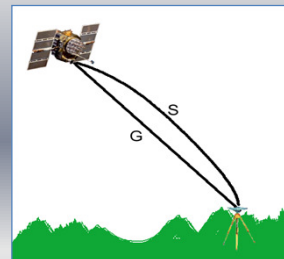
$$L = \int_S n ds$$

$$\Delta L = [\int_S n ds] - G = [\int_S (n - 1) ds] + (S - G)$$

$$\simeq \int_S (n - 1) ds$$

Propagation Delay

Curvature of the trajectory



$$\Delta L = 10^{-6} \int_S N ds \quad N = 10^6 (n - 1)$$

Refractivity

$$N = k_1 R_d \rho + R_v \left[ k_2' + \frac{k_3}{T} \right] \rho_{eau}$$

Density of total air

Density of water vapor

## Tropospheric Delay (2) – Decomposition

➤ Dry and Wet component

**Hydrostatic Delay (ZHD)**

- ~ 2,30 m at zenith
- slow time variation(1 cm / 6 h )
- function of ground pressure, and latitude of the site.

**Wet Delay (ZWD)**

- up to 20 cm in our latitudes at the zenith.
- highly correlated with weather data.
- function of temperature and density of water vapor along the signal path.

$$\Delta L_h^0 = 0.22768 \pm 0.0024 \frac{P_s}{f(\varphi, h)}$$

[Saastamoinen, 1973]

→ modeled

$$\Delta L_w = 10^{-6} R_v \int_S [k_2' + \frac{k_3}{T}] \rho_{eau} ds$$

→ Mesure de  $\rho_{eau}$  et T

**The water vapor delay (second term in refractivity) is not so easily integrated because of distribution of water vapor with height.**

## Correcting Tropospheric Errors (3) – Processing

Two opportunities to reduce Tropospheric errors within GPS measurements processing :

- 1

Correction of a priori hydrostatic delay (ZHD)  
+  
Estimation of Zenithal Wet tropospheric parameters Delay (ZWD) by Mean Squares fitting
- 2

Correction a priori or precise of hydrostatic Delay (ZHD)  
+  
External Correction of Slant Wet Delay (SWD) by steam measure instrument

## Tests and Results

To conduct our study, several tests were performed:

1. Baseline **ECRN-Murdjadjo**
2. Baseline **Algiers-Tamanrasset** (ALGEONET 1998)

Baseline ECRN-Murdjadjo

- ✓ short baseline (9km)
- ✓ Big slope Baseline (550km)

The Bernese is a processing GPS data software, developed at the University of Bern it's feature are :

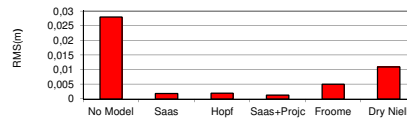
- Data processing of permanent networks.
- The determination of precise orbits.
- Parameter estimation of rotation of the earth.
- The calculation of an ionospheric model or the calibration antenna

## The variation of RMS based on the computational strategy

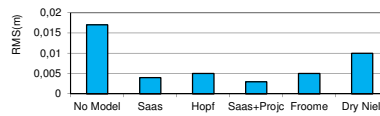
- **The strategies used are:**
  1. Without tropospheric model
  2. Saastamoinen without projection function
  3. Hopfield without projection function
  4. Saastamoinen with its projection function
  5. Essen and Froome
  6. The function of Dry Niell without a priori model

## RMS over Three components of the position 1. ECRN-Murdjadjio

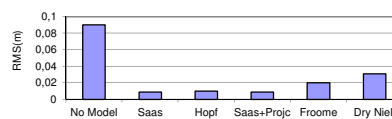
Altitude



Latitude

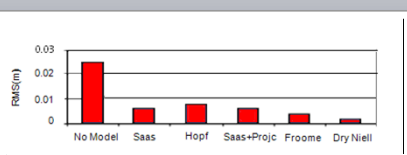


Longitude

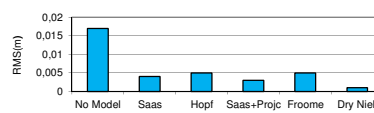


## RMS over Three components of the position 2. Algiers-Tamanrasset

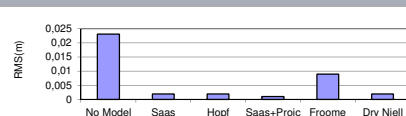
Altitude



Latitude

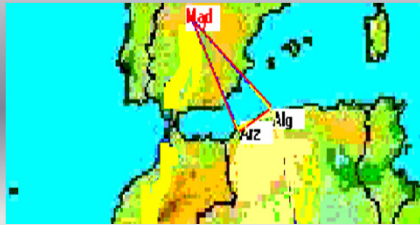


Longitude

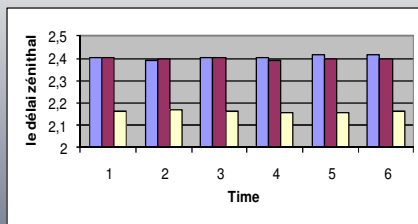




## Results of a permanent network (Algiers, Arzew and Madrid)



- ❖ The Base Algiers -Arzew (500km)
- ❖ The Base Algiers -Madrid (800km)



## Conclusions

- The tropospheric delay experienced by GPS signals affects the positioning accuracy.
- **Case of short baselines**
- The best results are obtained using the Saastamoinen model with its projection function..
- No-use of models with or without tropospheric features projections give less accurate results
- **Case of long baseline**
- No modeling of the troposphere, remove significantly the reference solution.

- For the two components, latitude and longitude, the two models Saatamoinen and Hopfield, with or without their projection functions gives almost the same results
- For the vertical component, using these two models with their duties projections can have the best result.
- Validate the results obtained on bases known on their exact components because the points coordinates relevant which we compared our results are themselves determined by GPS.
- Generalize the obtained conclusions through this work by using other data sets, with multiple configurations.